

Week 3 Practice

CSCI 567 Machine Learning

Spring 2025

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1. MULTIPLE-CHOICE QUESTIONS: One or more correct choice(s) for each question.

1.1. Which of the following surrogate losses is not an upper bound of the 0-1 loss?

(a) exponential loss: $\exp(-z)$

(b) hinge loss: $\max\{0, 1 - z\}$

(c) perceptron loss: $\max\{0, -z\}$

(d) logistic loss: $\ln(1 + \exp(-z))$

1.2. The perceptron algorithm makes an update $\mathbf{w}' \leftarrow \mathbf{w} + \eta y_n \mathbf{x}_n$ with $\eta = 1$ when \mathbf{w} misclassifies \mathbf{x}_n . Using which of the following different values for η will make sure \mathbf{w}' classifies \mathbf{x}_n correctly?

(a) $\eta > \frac{y(\mathbf{w}^T \mathbf{x}_n)}{\|\mathbf{x}_n\|_2^2}$

(b) $\eta < \frac{-y(\mathbf{w}^T \mathbf{x}_n)}{\|\mathbf{x}_n\|_2^2 + 1}$

(c) $\eta < \frac{-y(\mathbf{w}^T \mathbf{x}_n)}{\|\mathbf{x}_n\|_2^2}$

(d) $\eta > \frac{-y(\mathbf{w}^T \mathbf{x}_n)}{\|\mathbf{x}_n\|_2^2}$

1.3. Which of the following is true?

(a) Normalizing the output \mathbf{w} of the perceptron algorithm so that $\|\mathbf{w}\|_2 = 1$ changes its test error.

(b) Normalizing the output \mathbf{w} of the perceptron algorithm so that $\|\mathbf{w}\|_1 = 1$ changes its test error.

(c) When the data is linearly separable, logistic loss (without regularization) does not admit a minimizer.

(d) Minimizing 0-1 loss is generally NP-hard.

1.4. Which of the following statement is correct for function $f(\mathbf{w}) = w_1w_2$?

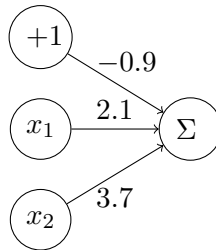
- (a) $(0, 0)$ is the only stationary point.
- (b) $(0, 0)$ is a local minimizer.
- (c) $(0, 0)$ is a local maximizer.
- (d) $(0, 0)$ is a saddle point.

2. Perceptron

Consider the following training dataset:

\mathbf{x}	y
(0, 0)	-1
(0, 1)	-1
(1, 0)	-1
(1, 1)	1

and a perceptron with weights $(w_0, w_1, w_2) = \{-0.9, 2.1, 3.7\}$



2.1. What is the accuracy of the perceptron on the training data?

\mathbf{x}	y	\hat{y}	$\mathbb{I}(y = \hat{y})$
(0, 0)	-1	$\text{sgn}(-0.9) = -1$	Y
(0, 1)	-1	$\text{sgn}(-0.9 + 3.7) = 1$	N
(1, 0)	-1	$\text{sgn}(-0.9 + 2.1) = 1$	N
(1, 1)	1	$\text{sgn}(-0.9 + 2.1 + 3.7) = 1$	Y

2.2. Select $\mathbf{x} = (1, 0)$ and $y = -1$. Use the perceptron training rule with $\eta = 1$ to train the perceptron for one iteration. What are the weights after this iteration?

2.3. What is the accuracy of the perceptron on the training data after this iteration? Does the accuracy improve?

\mathbf{x}	y	\hat{y}	$\mathbb{I}(y = \hat{y})$
(0, 0)	-1	$sgn(-1.9) = -1$	Y
(0, 1)	-1	$sgn(-1.9 + 3.7) = 1$	N
(1, 0)	-1	$sgn(-1.9 + 1.1) = -1$	Y
(1, 1)	1	$sgn(-1.9 + 1.1 + 3.7) = 1$	Y

3. Maximum Likelihood Estimation

A random sample set X_1, X_2, \dots, X_n of size n is taken from a Poisson distribution with a mean of $\lambda > 0$. As a reminder, a Poisson distribution is a discrete probability distribution over the natural numbers, with the following probability mass function

$$P(X = x) = \frac{\lambda^x \cdot e^{-\lambda}}{x!}, \quad \forall x \in \{0, 1, 2, \dots, \}$$

3.1. Find the log likelihood of the data; call it $l(\lambda)$. You may use any log base you want.

3.2. Find the maximum likelihood estimator for λ .